



# Abstract

This presentation describes in detail how mathematical probability is used to investigate the practicability of a proposed metric pertaining to a higher education funding formula model.

# Outline

- Proposed Metric
- Implementation
- Example
- Discussion
- Summary
- Q&A

## Proposed Metric

Release the set aside for next year iff the proportion of this year's graduates who are **successful** exceeds last year's proportion by more than 0.01 (= 1.0%).

# Proposed Metric

Release the set aside for ~~next year~~ year after next iff the proportion of this year's graduates who are successful exceeds  $m.78 / \text{GSA} \text{ cs } 100 \text{ sc} @ \text{ year's}$

# Proposed Metric

$N_i$  No. of year 4 grads.

$G_i$  No. of year 4 grads enrolled in grad/prof school.

$W_i$  No. of year 4 grads working successfully.

$p_i = (G_i + W_i) / N_i$  Pop. proportion of “successful” year 4 grads.

$p_2 - p_1$  Change in consecutive pop. proportions.

Release the set-aside for year 4 iff  $p_2 - p_1 \geq \mu$  r ä.r s







## How to Proceed?

$R_i = N_i - G_i$  No. of unknown year grads.

$u_i = W_i / R_i$  Corres. proportion of unknown year grads.

$$W_i = u_i R_i$$

Solution #2: Survey a SRS of the  $R_i$  unknown year grads, observe the number of successful grads, estimate  $W_i$  by estimating  $u_i$  using  $x_i / n_i$ .

- Need ~100% response rate, but this seems more attainable here
- Statistical approach which promises to be less expensive.
- Allows one to quantify decision uncertainty.

## Solution #2: Probability Results

1.  $\hat{u} \equiv \frac{x}{n}$

2.

3.

4.

## Solution #2: Probab

5.  $\hat{p} \sim \text{Normal}$

6.  $n$  —  
s —  
u

7.  $p \parallel r z_{\phi t}$

## Solution #2: Probability Results (cont.)

8.  $(\hat{p}_2)$

9.

10.

## Solution #2: Hypothesis Test

Hypotheses:

$$H_0: \mu_t = \mu_s \text{ dr ä r s}$$

$$H_A: \mu_t \neq \mu_s \text{ r ä r s}$$

Decision Rule: Reject the null hypothesis (i.e., **release the year 4 set aside**) at the approx.  $\alpha$  level of significance if

$$Z = \frac{\bar{p}_t - \bar{p}_s}{\sqrt{\frac{\hat{p}_t(1-\hat{p}_t)}{n_t} + \frac{\hat{p}_s(1-\hat{p}_s)}{n_s}}} > z_{\alpha/2} \text{ s ä x v w}$$

## Solution #2: Steps

1. Learn the no. of year 1 grads:
2. Learn the no. of year 1 grads in grad/prof school:
3. Determine the sample size for the survey of year 1 grads:
4. Survey SRS( ) of the year 1 grads,...
5. ...follow up, etc., ...
6. ...and compute the estimated proportion of year 1 grads who are “successful”:



## Solution #2: Example (cont.)

|                                  | FY2011 | FY2012 |                     |
|----------------------------------|--------|--------|---------------------|
| N No. graduates                  | 2,092  | 1,963  |                     |
| G No. in grad/prof school        | 585    | 549    | Assume 28% of N     |
| R = N - G Therest                | 1,507  | 1,414  |                     |
| n Sample size                    | 1,402  | 1,321  | Target m.e. = 0.005 |
| $u = W / R$                      |        |        |                     |
| X No. successful grads in sample | 1,000  | 975    | For example         |
| $\text{est}(u) = x / n$          | 0.7133 | 0.7381 |                     |
| $\text{est}(p)$                  | 0.7934 | 0.8113 |                     |
| m.e. for p                       | 0.0045 | 0.0044 |                     |
| $\text{est}(p_2 - p_1)$          |        | 0.0179 |                     |
| m.e. for $(p_2 - p_1)$           |        | 0.0063 |                     |
| Z                                |        | 2.465* | Release \$\$\$      |



## Solution #2: Remarks

1. Straightforward application of basic mathematical statistics and probability theory.
  - Straightforward implementation of the proposed funding formula metric.
  - Provides, additionally, a statement of uncertainty.

2. Show me success!

3. Practic      G ìá   tp U X € tì   ŒãÃ YCPĐÀ 0

3. 0 19.98 -198<00 47a|1 Tf .2e í ™İP – ' †\$Añ@ ,Q€   Â\*%oÀ

## Solution #2: Remarks (cont.)

5. The real metric: Release the set aside for **year after next** iff this year's **3 year weighted proportion** of graduates who are **successful** exceeds last year's **3 year weighted proportion** by more than 0.001 (=0.10%).

$$p_u \left\{ \frac{G_s W_s \quad G_t W_t \quad G_u W_u}{N_s \quad N_t \quad N_u} \right.$$

$$p_v \left\{ \frac{G_t W_t \quad G_u W_u \quad G_v W_v}{N_t \quad N_u \quad N_v} \right.$$

Release the set aside for **year 6** iff  $p_4 - p_3 \geq \mu$  r ä r.r s

# Summary

- Described a (distilled version of a) funding formula metric.
- Motivated and described a solution for implementing this metric, developed from mathematical probability.
- Presented examples.
- Critiqued this solution.

# Questions

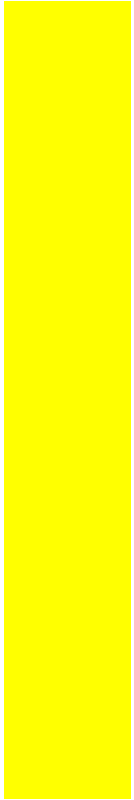
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.960 for 95% confidence (Usually used when reporting a "margin of error.")

.645 for 90% confidence



BACHELOR'S

NOTE:Usez=1  
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 NOTE:Usez=1

Required  
 increase in p  
 to satisfy or = 116EV M = 10 \$1#2D0= 108 0.5

PUBLIC BACCALAUREATE AND  
HIGHER DEGREE GRANTING  
INSTITUTIONS

| FY12 Total (N) | NSQ per r<br>student cost<br>(\$/student) | NSC Total<br>Cost(\$) | % Going on to<br>Grad or Prof<br>School | No. Going On<br>to PostBacc<br>(G) | No.<br>Potentially<br>Employed<br>(R=N G) |
|----------------|---|-----------------------|---|------------------------------------|---|
|----------------|---|-----------------------|---|------------------------------------|---|



|  |                         |                   |                          |                                   |                              |                              |                            |                                     |                                |                       |
|--|-------------------------|-------------------|--------------------------|-----------------------------------|------------------------------|------------------------------|----------------------------|-------------------------------------|--------------------------------|-----------------------|
| .960 for 95% confidence (Usually used when reporting a "margin of error.") |                         |                   |                          |                                   |                              |                              |                            |                                     |                                |                       |
| .645 for 90% confidence  |                         |                   |                          |                                   |                              |                              |                            |                                     |                                |                       |
| .283 for 80% confidence  |                         |                   |                          |                                   |                              |                              |                            |                                     |                                |                       |
| Best prior guess for u (use 0.5 to be maximally conservative)              | Optimal Sample Size (n) | Sampling Fraction | Cost Initial Survey (\$) | Total Cost Initial Data Gathering | Response Rate Initial Survey | Size of 1st Follow up Survey | Cost of 1st Follow up (\$) | Total Cost After 1st Follow up (\$) | Response Rate of 1st Follow up | Size of 2nd Follow up |
| 0.50   |                         |                   | 6                        |                                   | 45%                          |                              | 6                          |                                     | 60%                            |                       |
| 0.50   | 116                     | 1.0000            | 696                      | 715                               | 0.45                         | 64                           | 384                        | 1,099                               | 0.60                           | 26                    |
| 0.50   | 216                     | 0.9908            | 1,296                    | 1,332                             | 0.45                         | 119                          | 714                        | 2,046                               | 0.60                           | 48                    |
| 0.50   | 605                     | 0.9711            | 3,630                    | 3,734                             | 0.45                         | 333                          | 1,998                      | 5,732                               | 0.60                           | 134                   |
| 0.50   | 2,081                   | 0.8958            | 12,486                   | 12,873                            | 0.45                         | 1,145                        | 6,870                      | 19,743                              | 0.60                           | 458                   |
| 0.50   | 747                     | 0.9626            | 4,482                    | 4,611                             | 0.45                         | 411                          | 2,466                      | 7,077                               | 0.60                           | 165                   |
| 0.50   | 498                     | 0.9765            | 2,988                    | 3,073                             | 0.45                         | 274                          | 1,644                      | 4,717                               | 0.60                           | 110                   |
| 0.50   | 795                     | 0.9613            | 4,770                    | 4,908                             | 0.45                         | 438                          | 2,628                      | 7,536                               | 0.60                           | 176                   |
| 0.50   | 1,124                   | 0.9445            | 6,744                    | 6,942                             | 0.45                         | 619                          | 3,714                      | 10,656                              | 0.60                           | 248                   |
| 0.50   | 885                     | 0.9557            | 5,310                    | 5,464                             | 0.45                         | 487                          | 2,922                      | 8,386                               | 0.60                           | 195                   |
| 0.50   | 1,265                   | 0.9370            | 7,590                    | 7,815                             | 0.45                         | 696                          | 4,176                      | 11,991                              | 0.60                           | 279                   |
| 0.50   | 3,319                   | 0.8337            | 19,914                   | 20,577                            | 0.45                         | 1,826                        | 10,956                     | 31,533                              | 0.60                           | 731                   |
| 0.50   | 1,186                   | 0.9413            | 7,116                    | 7,326                             | 0.45                         | 653                          | 3,918                      | 11,244                              | 0.60                           | 262                   |
| 0.50   | 1,321                   | 0.9342            | 7,926                    | 8,162                             | 0.45                         | 727                          | 4,362                      | 12,524                              | 0.60                           | 291                   |